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ON THE RELATION BETWEEN G_2^\ast STRUCTURES AND ALMOST PARACONTACT STRUCTURES

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Abstract. In this manuscript, we investigate the possible classes of seven-dimensional almost paracontact metric structures induced by the three-forms of G_2^* structures. We write the projections that determine to which class the almost paracontact structure belongs, by using the properties of the G_2^* structures. Then we study the properties that the characteristic vector field of the almost paracontact metric structure should have such that the structure belongs to a specific subclass of almost paracontact metric structures.

MSC: 53C25, 53D10 Keywords: Almost paracontact metric structure, G_2^* structure, normal structure, paracontact structure

1. Introduction

Manifolds with almost paracontact structures were first defined by Kaneyuki and Williams in [3]. Zamkovoy provided all the technical apparatus needed in [8]. After these remarkable works, almost paracontact metric manifolds were written as a direct sum of 12 subspaces with respect to the symmetry properties of the Levi-Civita covariant derivative of the fundamental two-form in [5,9].

Almost paracontact metric structures induced by manifolds with G_2^* structures were constructed in [6] and existence of some classes were investigated. Our aim in this study is to get further results by calculating projections given in [9] on each of twelve subspaces of almost paracontact metric structures. Also, we provide some examples.

2. Preliminaries

Consider \mathbb{R}^7 with the metric $g_{4,3}$ having the signature (-, -, -, -, +, +, +). The group G_2^* is defined as

$$G_2^* = \{ g \in \mathrm{GL}(7, \mathbb{R}); \, g^* \varphi = \varphi \}$$

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