Contents

Preface xi

CHAPTER 1 INTRODUCTION 1

- 1.1 Variability and the Need for Statistics 1
- 1.2 Systematic Versus Random Variability 3
- 1.3 Érror Variance Again 5
- 1.4 Reducing Error Variance 5
- 1.5 Overview of the Book 7
- 1.6 Concluding Remarks 7

CHAPTER 2 LOOKING AT DATA: UNIVARIATE DISTRIBUTIONS 10

- 2.1 Introduction 10
- 2.2 Exploring a Single Sample 11
- 2.3 Comparing Two Data Sets 18
- 2.4 Other Measures of Location and Spread: The Mean and Standard Deviation 20
- 2.5 Standardized (z) Scores 27
- 2.6 Measures of the Shape of a Distribution 28
- 2.7 Concluding Remarks 33

CHAPTER 3 LOOKING AT DATA: RELATIONS BETWEEN QUANTITATIVE VARIABLES 37

- 3.1 Introduction 37
- 3.2 Some Examples 37
- 3.3 Linear Relations 43
- 3.4 The Pearson Product-Moment Correlation Coefficient 44

- 3.5 Linear Regression 51
- 3.6 The Coefficient of Determination, r^2 54
- 3.7 Influential Data Points and Resistant Measures of Regression 55
- 3.8 Describing Nonlinear Relations 56
- 3.9 Concluding Remarks 56

CHAPTER 4 PROBABILITY AND THE BINOMIAL DISTRIBUTION 61

- 4.1 Introduction 61
- 4.2 Discrete Random Variables 62
- 4.3 Probability Distributions 63
- 4.4 Some Elementary Probability 67
- 4.5 The Binomial Distribution 75
- 4.6 Means and Variances of Discrete Distributions 79
- 4.7 Hypothesis Testing 80
- 4.8 Independence and the Sign Test 86
- 4.9 More About Assumptions and Statistical Tests 89
- 4.10 Concluding Remarks 89

CHAPTER 5 ESTIMATION AND HYPOTHESIS TESTS: THE NORMAL DISTRIBUTION 100

- 5.1 Introduction 100
- 5.2 Continuous Random Variables 100
- 5.3 The Normal Distribution 102
- 5.4 Point Estimates of Population Parameters 104
- 5.5 Inferences About Population Means: The One-Sample Case 112
- 5.6 Inferences About Population Means: The Correlated-Samples Case 117
- 5.7 The Power of the z Test 119
- 5.8 Hypothesis Tests and CIs 122
- 5.9 Validity of Assumptions 123
- 5.10 Comparing Means of Two Independent Populations 125
- 5.11 The Normal Approximation to the Binomial Distribution 128
- 5.12 Concluding Remarks 129

CHAPTER 6 ESTIMATION, HYPOTHESIS TESTS, AND EFFECT SIZE: THE *t* DISTRIBUTION 140

- 6.1 Introduction 140
- 6.2 Inferences About a Population Mean 141
- 6.3 The Standardized Effect Size 145
- 6.4 Power of the One-Sample *t* Test 147
- 6.5 The t Distribution: Two Independent Groups 152
- 6.6 Standardized Effect Size for Two Independent Means 156
- 6.7 Power of the Test of Two Independent Means 157
- 6.8 Assumptions Underlying the Two-Group t Test 158
- 6.9 Contrasts Involving More than Two Means 161
- 6.10 Correlated Scores or Independent Groups? 165
- 6.11 Concluding Remarks $16\hat{7}$

CHAPTER 7 THE CHI-SQUARE AND F DISTRIBUTIONS 173

- 7.1 Introduction 173
- 7.2 The χ^2 Distribution 174
- 7.3 Inferences About the Population Variance 175
- 7.4 The F Distribution 179
- 7.5 Inferences About Population Variance Ratios 182
- 7.6 Relations Among Distributions 185
- 7.7 Concluding Remarks 186

CHAPTER 8 BETWEEN-SUBJECTS DESIGNS: ONE FACTOR 191

- 8.1 Introduction 191
- 8.2 Exploring the Data 193
- 8.3 The Analysis of Variance 195
- 8.4 The Model for the One-Factor Design 201
- 8.5 Assessing the Importance of the Independent Variable 207
- 8.6 Power of the F Test 212
- 8.7 Assumptions Underlying the F Test 216
- 8.8 Concluding Remarks 227

CHAPTER 9 CONTRASTS AMONG MEANS 233

- 9.1 Introduction 233
- 9.2 Definitions and Examples of Contrasts 234
- 9.3 Calculations of the *t* Statistic for Testing Hypotheses About Contrasts 235
- 9.4 The Proper Unit for the Control of Type 1 Error 241
- 9.5 Planned Versus Post Hoc Contrasts 243
- 9.6 Controlling the FWE for Families of *K* Planned Contrasts 244
- 9.7 Testing All Pairwise Contrasts 247
- 9.8 Comparing a 1 Treatment Means with a Control: Dunnett's Test 255
- 9.9 Controlling the Familywise Error Rate for Post Hoc Contrasts 256
- 9.10 The Sum of Squares Associated with a Contrast 258
- 9.11 Concluding Remarks 260

CHAPTER 10 TREND ANALYSIS 267

- 10.1 Introduction 267
- 10.2 Linear Trend 268
- 10.3 Testing Nonlinear Trends 274
- 10.4 Concluding Remarks 280

CHAPTER 11 MULTIFACTOR BETWEEN-SUBJECTS DESIGNS: SIGNIFICANCE TESTS IN THE TWO-WAY CASE 284

- 11.1 Introduction 284
- 11.2 A First Look at the Data 285
- 11.3 Two-Factor Designs: The ANOVA 288
- 11.4 The Structural Model and Expected Mean Squares 295
- 11.5 Main Effect Contrasts 297

x CONTENTS

- 11.6 More About Interaction 298
- 11.7 Simple Effects 302
- 11.8 Two-Factor Designs: Trend Analysis 305
- 11.9 Concluding Remarks 309

CHAPTER 12 MULTIFACTOR BETWEEN-SUBJECTS DESIGNS: FURTHER DEVELOPMENTS 315

- 12.1 Introduction 315
- 12.2 Measures of Effect Size 315
- 12.3 Power of the F Test 318
- 12.4 Unequal Cell Frequencies 319
- 12.5 Three-Factor Designs 324
- 12.6 More than Three Independent Variables 332
- 12.7 Pooling in Factorial Designs 332
- 12.8 Blocking to Reduce Error Variance 335
- 12.9 Concluding Remarks 336

CHAPTER 13 REPEATED-MEASURES DESIGNS 342

- 13.1 Introduction 342
- 13.2 The Additive Model and Expected Mean Squares for the $S \times A$ Design 345
- 13.3 The Nonadditive Model for the $S \times A$ Design 352
- 13.4 Hypothesis Tests Assuming Nonadditivity 355
- 13.5 Power of the F Test 363
- 13.6 Multifactor Repeated-Measures Designs 363
- 13.7 Fixed or Random Effects? 371
- 13.8 Nonparametric Procedures for Repeated-Measures Designs 372
- 13.9 Concluding Remarks 377

CHAPTER 14 MIXED DESIGNS: BETWEEN-SUBJECTS AND WITHIN-SUBJECTS FACTORS 386

- 14.1 Introduction 386
- 14.2 One Between-Subjects and One Within-Subjects Factor 386
- 14.3 Rules for Generating Expected Mean Squares 392
- 14.4 Measures of Effect Size 394
- 14.5 Power Calculations 396
- 14.6 Contrasting Means in Mixed Designs 397
- 14.7 Testing Simple Effects 401
- 14.8 Pretest–Posttest Designs 402
- 14.9 Additional Mixed Designs 403
- 14.10 Concluding Remarks 407

CHAPTER 15 USING CONCOMITANT VARIABLES TO INCREASE POWER: BLOCKING AND ANALYSIS OF COVARIANCE 412

- 15.1 Introduction 412
- 15.2 Example of an ANCOVA 415

CONTENTS xi

- 15.3 Assumptions and Interpretation in an ANCOVA 422
- 15.4 Testing Homogeneity of Slopes 427
- 15.5 More About ANCOVA Versus Treatments × Blocks 428
- 15.6 Estimating Power in an ANCOVA 430
- 15.7 ANCOVA in Higher-Order Designs 431
- 15.8 Some Extensions of the ANCOVA 431
- 15.9 Concluding Remarks 432

CHAPTER 16 HIERARCHICAL DESIGNS 436

- 16.1 Introduction 436
- 16.2 Groups Within Treatments 437
- 16.3 Groups Versus Individuals 443
- 16.4 Extensions of the Groups-Within-Treatments Design 445
- 16.5 Items Within Treatments 449
- 16.6 Concluding Remarks 452

CHAPTER 17 LATIN SQUARES AND RELATED DESIGNS 457

- 17.1 Introduction 457
- 17.2 Selecting a Latin Square 459
- 17.3 The Single Latin Square 461
- 17.4 The Replicated Latin Square Design 469
- 17.5 Balancing Carry-Over Effects 474
- 17.6 Greco-Latin Squares 476
- 17.7 Concluding Remarks 477

CHAPTER 18 MORE ABOUT CORRELATION 480

- 18.1 Introduction 480
- 18.2 Further Issues in Understanding the Correlation Coefficient 481
- 18.3 Inference About Correlation 489
- 18.4 Partial Correlations 501
- 18.5 Other Measures of Correlation 504
- 18.6 Concluding Remarks 511

CHAPTER 19 MORE ABOUT BIVARIATE REGRESSION 519

- 19.1 Introduction 519
- 19.2 Regression Toward the Mean 520
- 19.3 Inference in Linear Regression 522
- 19.4 An Example: Regressing Cholesterol Level on Age 532
- 19.5 Checking for Violations of Assumptions 534
- 19.6 Locating Outliers and Influential Data Points 542
- 19.7 Testing Independent Slopes for Equality 548
- 19.8 Repeated-Measures Designs 549
- 19.9 Multilevel Modeling 551
- 19.10 Concluding Remarks 551

CHAPTER 20 MULTIPLE REGRESSION 562

- 20.1 Introduction 562
- 20.2 A Regression Example with Several Predictor Variables 563
- 20.3 The Nature of the Regression Coefficients 572
- 20.4 The Multiple Correlation Coefficient and the Partitioning of Variability in Multiple Regression 573
- 20.5 Inference in Multiple Regression 580
- 20.6 Selecting the Best Regression Equation for Prediction 591
- 20.7 Explanation Versus Prediction in Regression 593
- 20.8 Testing for Curvilinearity in Regression 598
- 20.9 Including Interaction Terms in Multiple Regression 601
- 20.10 Multiple Regression in Repeated-Measures Designs 607
- 20.11 Concluding Remarks 608

CHAPTER 21 REGRESSION WITH CATEGORICAL AND QUANTITATIVE VARIABLES: THE GENERAL LINEAR MODEL 614

- 21.1 Introduction 614
- 21.2 One-Factor Designs 615
- 21.3 Regression Analyses and Factorial Designs 621
- 21.4 Using Categorical and Continuous Variables in the Same Analysis 630
- 21.5 Coding Designs with Within-Subjects Factors 634
- 21.6 Concluding Remarks 637

APPENDIXES

- Appendix A Notation and Summation Operations 641
- Appendix B Expected Values and Their Applications 649
- Appendix C Statistical Tables 653

Answers to Selected Exercises 685

- Endnotes 721
- References 729
- Author Index 743
- Subject Index 749