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## *N*-WAVE TYPE SYSTEMS AND THEIR GAUGE EQUIVALENT RELATED TO THE ORTHOGONAL ALGEBRAS

## VLADIMIR GERDJIKOV<sup>†</sup>, GEORGI GRAHOVSKI<sup>†</sup> and NIKOLAY KOSTOV<sup>‡</sup>

<sup>†</sup> Institute for Nuclear Research and Nuclear Energy Bulgarian Academy of Sciences, 1784 Sofia, Bulgaria

<sup>‡</sup> Institute of Electronics, Bulgarian Academy of Sciences 1784 Sofia, Bulgaria

> Abstract. The reductions of the integrable N-wave type equations solvable by the inverse scattering method with the generalized Zakharov-Shabat system L and related to some simple Lie algebra  $\mathfrak{g}$ are analyzed. Special attention is paid to the  $\mathbb{Z}_2$ -reductions including ones that can be embedded also in the Weyl group of  $\mathfrak{g}$ . The consequences of these restrictions on the structure of the dresing factors are outlined. An example of 4-wave equations (with application to nonlinear optics) and its gauge equivalent are given.

## 1. Introduction

The aim of the present paper is to study the class of N-wave equations [1, 8, 11–13], their generalizations to simple Lie algebras [2, 5] and their gauge equivalent ones extending the results in [6]. We describe their scattering data, dressing factors, 1-soliton solutions and outline some of their reductions.

The N-wave type equations related to the simple Lie algebras can be solved by applying the inverse scattering method for the generalized Zakharov–Shabat system [5]:

$$L(\lambda)\psi \equiv \left(i\frac{d}{dx} + [J,Q(x,t)] - \lambda J\right)\psi(x,t,\lambda) = 0$$
(1)

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